

# Dynamic Methods in Macroeconomics

Lectures: 25 hours

Excercises: 3x2 hours

Prerequisites: Macroeconomic theory

## Description

The aim of the course is to provide a solid overview of recursive methods and familiarize students with their use in macroeconomics. The course focuses mainly on discrete time dynamic programming and its economic applications. A brief sketch on continuous time optimization models will be given. The course covers numerical methods for solving dynamic optimization problems.

## Main Text books

N. Stokey and R. Lucas with E. Prescott. Recursive methods in economic dynamics. Harvard University Press, 1989. (SLP)

L. Ljungqvist and T. Sargent. Recursive macroeconomic theory. MIT Press, 2000. (LS)

## Course Requirements and Exams

Final grade consists of exam and exercise points. Exercises are not mandatory for passing the course but the exercise points determine 25 % of the final grade.

## Preliminary course outline

### I Theory of dynamic programming

1. Introduction to dynamic programming

Example: optimal growth

Sequential formulation vs. recursive formulation

Idea of solving

Material: SLP chapter 2

2. Mathematical background

Normed vector spaces

Correspondences

Contraction mapping theorem, Blackwell's theorem

Material: SLP chapter 3

3. Principle of optimality

Formal analysis of the dynamic programming problem

Bellman equation, one-shot deviation principle

Solving by value function iteration and policy iteration

Euler equations

Material: SLP chapter 4

4. Stochastic dynamic programming  
Introduction to Markov processes  
Principle of optimality for stochastic problems  
Necessary and sufficient optimality conditions  
Principle of certainty equivalence  
Material: SLP chapters 8 and 9, LS chapters 1 and 2

## **II Applications**

5. Growth (different variants), investment, inventory, etc.  
Material: SLP chapter 5, LS chapter 11

6. Competitive storage  
Material: Deaton, A., and G. Laroque, On the Behaviour of Commodity Prices, Review of Economics Studies, 59, 1992

7. Job search and optimal stopping  
Material: J. J. McCall, Economics of Information and Job Search, The Quarterly Journal of Economics, 84(1), 1970, SLP 10, LS chapter 5 (pp. 81—94)

8. Self-Enforcing Contracts  
Thomas, J., and T. Worrall. Self-Enforcing Wage Contracts, Review of Economic Studies, 55 (4), 1988

## **II Numerical dynamic programming**

8. Numerical methods  
Numerical optimization  
Function approximation  
Introduction to Matlab  
Material: LS chapter 3

9. Practical dynamic programming  
Dynamic programming algorithm  
Implementing value function and policy iterations  
Introduction to CompEcon/Matlab  
Material: LS chapter 3

## **III Continuous Time Models**

10. Bellman equation for continuous time models  
Pontryagin's maximum principle  
Economic growth in continuous time, Tobin's q  
D. Acemoglu. Introduction to Modern Economic Growth. 2007 (Section 7.3)

11. Application: Kiyotaki-Wright model in continuous time  
Material: Kiyotaki, N., and R. Wright, A Search-Theoretic Approach to Monetary Economics, American Economic Review, 83(3), 1993